

**III B.Tech I Semester Regular Examinations, Nov/Dec 2009**  
**DESIGN AND ANALYSIS OF ALGORITHMS**  
**Computer Science And Engineering**

**Time: 3 hours****Max Marks: 80**

**Answer any FIVE Questions**  
**All Questions carry equal marks**

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1. (a) Explain the Prim's algorithm with the appropriate example.  
(b) Write the Prim's algorithm to find the minimum spanning tree. [8+8]
2. (a) Describe some classic NP problems and why they are important.  
(b) Write about tractable and intractable problems. [8+8]
3. (a) Modify the Binary search of the text so that in the case of unsuccessful search it returns the index  $i$  such that  $k(i) < key < k(i+1)$ .  
(b) Is Quick sort a stable sorting method? Justify your answer. [8+8]
4. Show that the relation "V and W lie in the same biconnected component of G" is not an equivalence relation. [16]
5. Write an algorithm schema FifoBB for a FIFO branch-and-bound search for a least-cost answer node. [16]
6. With a numerical example, explain Dynamic Partitioning Scheme that can be adopted in solving 0/1 Knapsack Problem using Back tracking method. [16]
7. (a) Given a sequence of  $n$  real numbers  $A(1), \dots, A(n)$ , write a procedure to determine a contiguous subsequence  $A(i), \dots, A(j)$  for which the sum of elements in the subsequence is maximized.  
(b) You are given  $n$  types of coin denominations of values  $v(1) < v(2) < \dots < v(n)$  (all integers). Assume  $v(1) = 1$ , so you can always make change for any amount of money  $C$ . Give an algorithm which makes change for an amount of money  $C$  with as few considerations as possible. [8+8]
8. Let  $a, b, c$  be numbers such that  $0 \leq a, b < 1$ , and  $c > 0$ . Let  $T(n)$  be defined by  $T(n) = T(an) + T(bn) + cn$ .  
(a) Show that if  $(a+b) < 1$  then  $T(n)$  is bounded by linear function.  
(b) Does there exist a  $d$  such that, for all  $a, b, c$  above,  $T(n) = O(n^d)$ ? [16]

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